

Digital Outputs of an 8-Bit 1.5-Bit/Stage ADC

$$V_{in} = +0.8 \text{ LSB} \Rightarrow V_{res1} = 2V_{in} = 1.6 \text{ LSB} \Rightarrow D_1 = D_1$$

$$V_{res2} = 4V_{in} = 3.2 \text{ LSB} \Rightarrow D_1 = D_2$$

$$V_{res3} = 8V_{in} = 6.4 \text{ LSB} \Rightarrow D_1 = D_3$$

$$V_{res4} = 16V_{in} = 12.8 \text{ LSB} \Rightarrow D_1 = D_4$$

$$V_{res5} = 32V_{in} = 25.6 \text{ LSB} \Rightarrow D_1 = D_5$$

$$V_{res6} = 64V_{in} = 51.2 \text{ LSB} \Rightarrow D_1 = D_6$$

$$V_{res7} = 128V_{in} - V_R = -25.6 \text{ LSB} \Rightarrow D_1 = D_7$$

$$D_1 = D_0$$

$$\left. \begin{aligned} D_{out} &= D_0 + D_1 2^{-1} + D_2 2^{-2} + D_3 2^{-3} \\ &\quad + D_4 2^{-4} + D_5 2^{-5} + D_6 2^{-6} \\ &\quad + D_7 2^{-7} \\ \Rightarrow D_{outT} &= \begin{array}{r} 0 \\ + \\ 0 \\ + \\ 0 \\ + \\ 0 \\ + \\ 0 \end{array} \\ &\quad \begin{array}{r} 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 0 \end{array} \\ \hline D_{outT} &= 10000000 \end{aligned} \right\}$$

$$\Rightarrow D_{outT} = 128$$

$$V_{in} = -0.8 \text{ LSB} \Rightarrow V_{res1} = 2V_{in} = -1.6 \text{ LSB} \Rightarrow D_1 = D_1$$

$$V_{res2} = 4V_{in} = -3.2 \text{ LSB} \Rightarrow D_1 = D_2$$

$$V_{res3} = 8V_{in} = -6.4 \text{ LSB} \Rightarrow D_1 = D_3$$

$$V_{res4} = 16V_{in} = -12.8 \text{ LSB} \Rightarrow D_1 = D_4$$

$$V_{res5} = 32V_{in} = -25.6 \text{ LSB} \Rightarrow D_1 = D_5$$

$$V_{res6} = 64V_{in} = -51.2 \text{ LSB} \Rightarrow D_1 = D_6$$

$$V_{res7} = 128V_{in} + V_R = 25.6 \text{ LSB} \Rightarrow D_1 = D_7$$

$$\left. \begin{aligned} D_{out} &= \begin{array}{r} 0 \\ + \\ 0 \\ + \\ 0 \\ + \\ 0 \\ + \\ 0 \end{array} \\ &\quad \begin{array}{r} 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \end{array} \\ \hline D_{outT} &= 01111111 \end{aligned} \right\}$$

$$\Rightarrow D_{outT} = 127$$

$$V_{in} = +32.8 \text{ LSB} \Rightarrow V_{res1} = (2V_{in} - V_R) = -62.4 \text{ LSB} \Rightarrow D_0 = D_0$$

$$V_{res2} = (2V_{res1} + V_R) = 3.2 \text{ LSB} \Rightarrow D_1 = D_2$$

$$V_{res3} = 2V_{res2} = 6.4 \text{ LSB} \Rightarrow D_1 = D_3$$

$$V_{res4} = 2V_{res3} = 12.8 \text{ LSB} \Rightarrow D_1 = D_4$$

$$V_{res5} = 2V_{res4} = 25.6 \text{ LSB} \Rightarrow D_1 = D_5$$

$$V_{res6} = 2V_{res5} = 51.2 \text{ LSB} \Rightarrow D_1 = D_6$$

$$V_{res7} = 2V_{res6} - V_R = -25.6 \text{ LSB} \Rightarrow D_1 = D_7$$

$$\left. \begin{aligned} D_{outT} &= \begin{array}{r} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \\ &\quad \begin{array}{r} 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{array} \\ \hline D_{outT} &= 10100000 \end{aligned} \right\}$$

$$\Rightarrow D_{outT} = 160$$