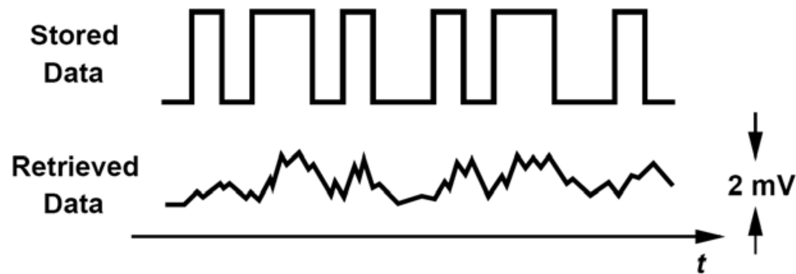
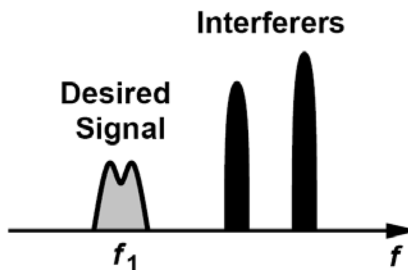
Why Analog?

- **Naturally-occurring signals, e.g., voice and video, are analog.**
- **System and medium non-idealities often make it necessary to treat <u>digital</u> signals as analog:**

- **Data Retrieved from Disk**



- **Digital Wireless Communications**



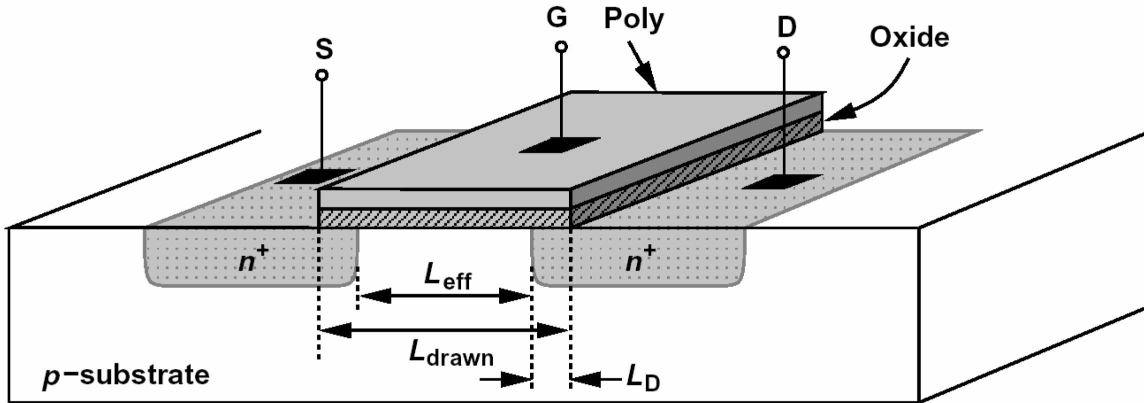
<u>Why is analog design such a big deal?</u>

- **Entails more trade-offs than digital design:**

- **More sensitive to noise and cross-talk.**
- **More sensitive to second-order effects in devices.**
- **More difficult to automate.**
- **More difficult to model and simulate.**
- **We want to design analog circuits in mainstream VLSI technologies, e.g., CMOS, with no additional processing steps, trimming, factory calibration, etc.**

REVIEW OF MOS DEVICES

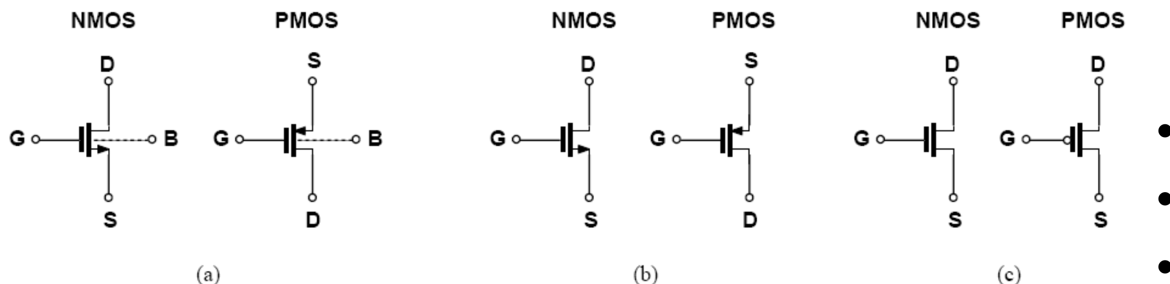
MOS Structure (NMOS)



- A piece of polysilicon with a width of W and length of L on top of a thin layer of oxide defines the gate area.
- Source and drain areas are heavily doped.
- Substrate usually tied to the most negative voltage.
- $L_{eff} = L - 2L_D$, where L_D is the side diffusion of source and drain.

MOS Symbols (Enhancement Type)

PMOS **NMOS**

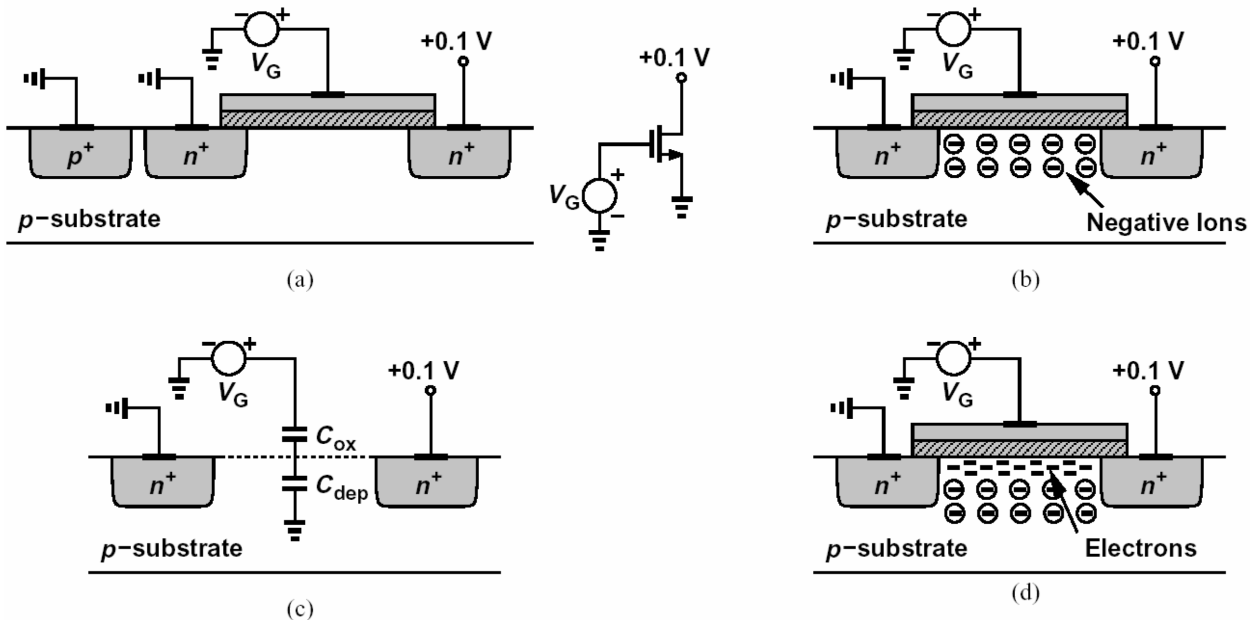


- MOS structure is symmetric.
- MOS devices have a very high input impedance.

MOS characteristics

- How does the device turn on and off?
- What is the drain-source current when the device is on?

Threshold Voltage



- For $V_{GS} < V_{TH}$, holes in substrate are repelled from gate area, leaving negative ions behind. (No current flows because no carriers are available.)
  → A depletion region forms under the gate.

- For $V_{GS} \approx V_{TH}$, electrons are attracted to the interface under gate, establishing a "channel" for conduction. The channel is also called the "inversion layer."

- For $V_{GS} \approx V_{TH}$, depletion region under channel remains relatively constant, but the charge in inversion layer increases . ↑
- Turn-on process not really abrupt, i.e., for $V_{GS} \approx V_{TH}$, $I_D > 0$. => Sub-threshold conduction (considered later).

- For a long-channel device with uniform substrate doping:
(and $V_{sub} = V_{source}$):

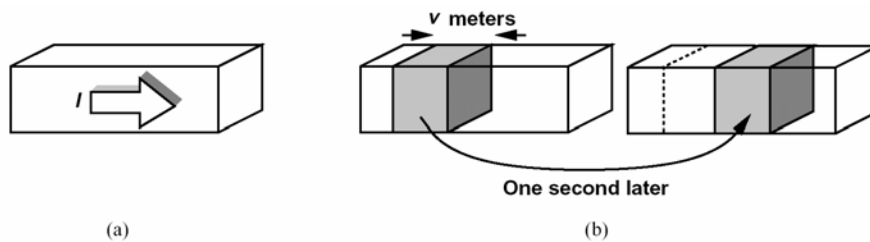
$$V_{TH} = \Phi_{MS} + 2\Phi_F + \frac{Q_{dep}}{C_{ox}}$$

where $\Phi_F = (kT/q)\ln(N_{sub}/n_i)$ $Q_{dep} = \sqrt{4q\epsilon_{si}|\Phi_F|N_{sub}}$

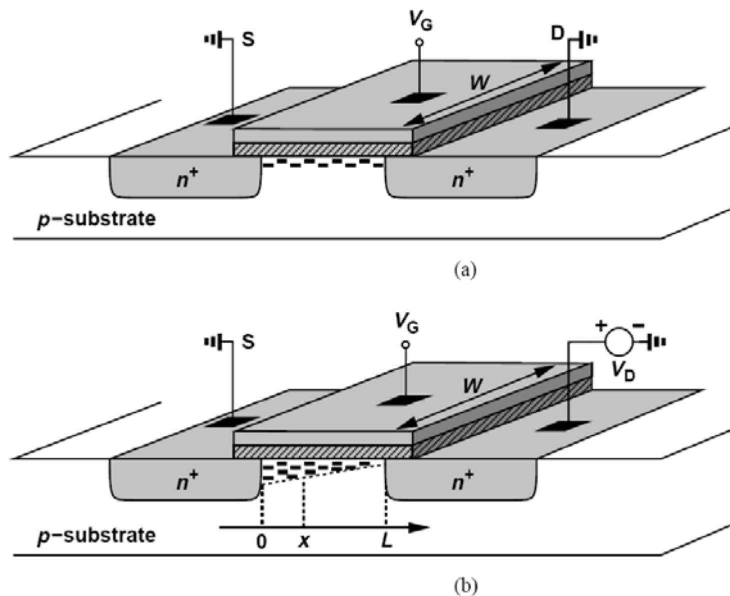
- **Often need to implant the channel to obtain the "right" threshold.**

- **A helpful approximation: For $V_{GS} \approx V_{TH}$, there is only depletion region in the gate area; for $V_{GS} \approx V_{TH}$, the depletion region is constant and the inversion layer charge increases.**

- **A useful Lemma: If a conductor carries a constant current *I* and it has a charge density (charge per unit length) of Q_d and the charge moves with a velocity *v*:** $I = Q_d\, v$



MOS I – V Characteristics



- **For V_{DS} > o, the inversion layer charge is non-uniform:**

$$Q_d(x) = WC_{ox}[V_{GS} - V(x) - V_{TH}]$$

Note that as we approach the end of the channel, the charge density falls.

- **To find the current, multiply charge density by charge velocity. For a semiconductor:**

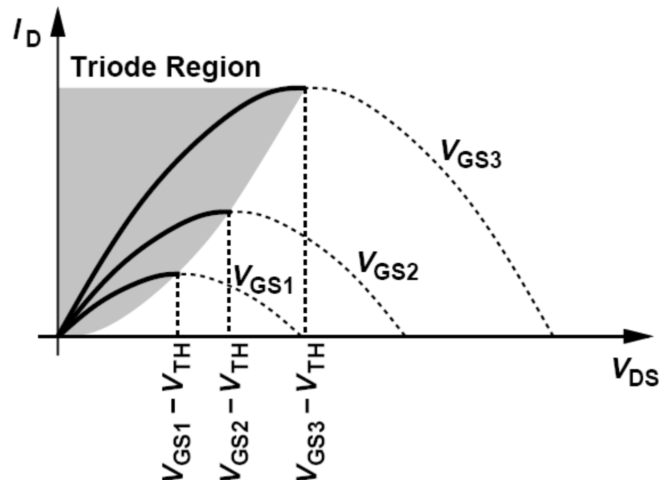
The drain current is therefore given by

$$I_D = WC_{ox}[V_{GS} - V(x) - V_{TH}]\mu_n \frac{dV(x)}{dx}$$

subject to boundary conditions at the two ends of the channel. Thus,

$$\int_{x=0}^{L} I_D dx = \int_{V=0}^{V_{DS}} WC_{ox}\mu_n[V_{GS} - V(x) - V_{TH}]dx$$

and hence,

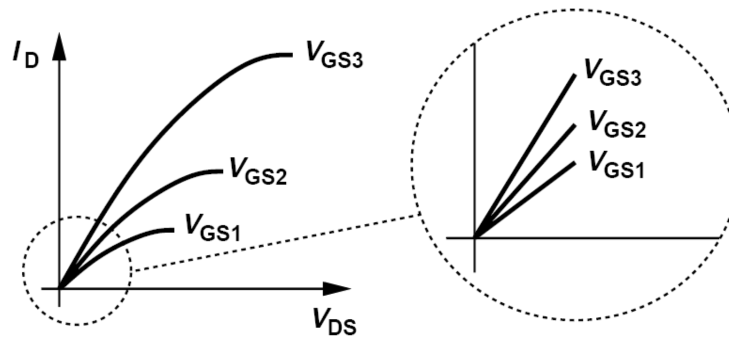


- **Assumptions made:**

1. **One-dimensional structure**
2. **Constant mobility**
3. **Constant depletion layer charge**

  - **For small V_{DS},**

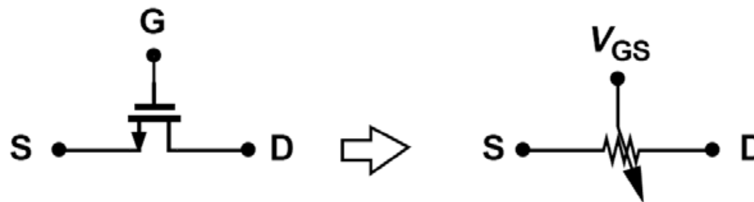
$$I_D \approx \mu_n C_{ox}\frac{W}{L}(V_{GS} - V_{TH})V_{DS}$$



Each line represents an ohmic resistor of

$$R_{on} =$$

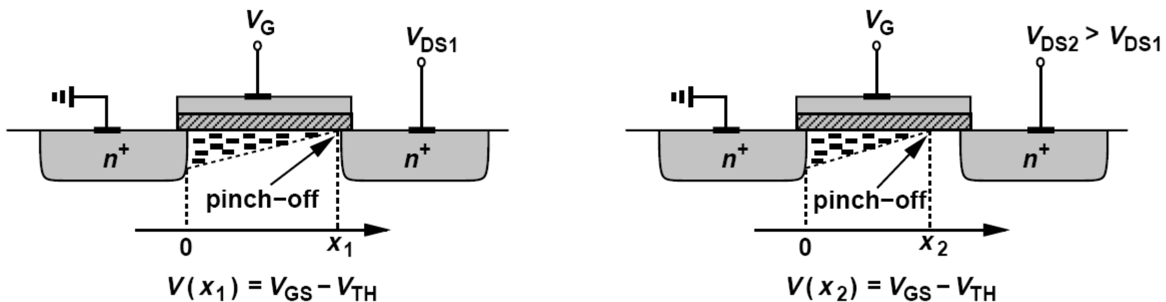
Thus, a MOS device can operate as a resistor whose value is controlled by V_{GS} (so long as V_{DS} << 2 ($V_{GS} \approx V_{TH}$):



- **Note that the device can be on but have zero current, which occurs only if V_{DS} = o.**

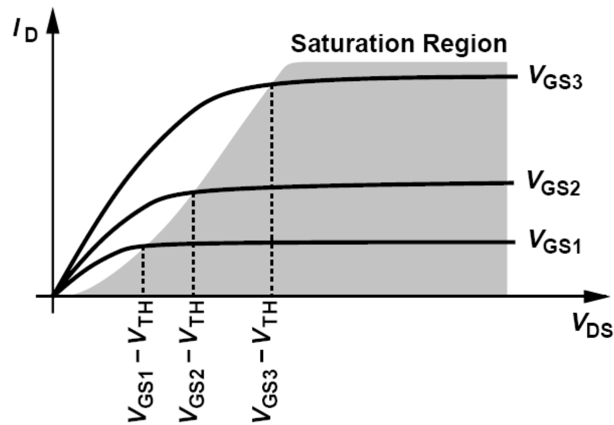
Pinch-Off

- **What happens if $V_{DS} > V_{GS} - V_{TH}$?**

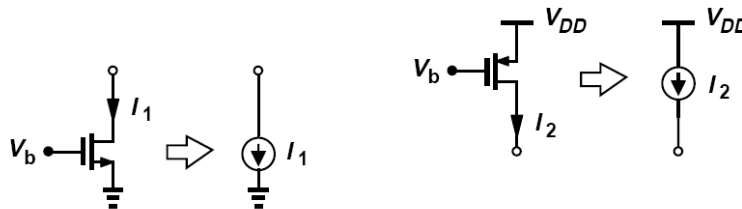


- **Electrons reach a high velocity near the end of inversion layer and shoot into depletion region around the drain.**

- **Device has entered "Saturation Region."**

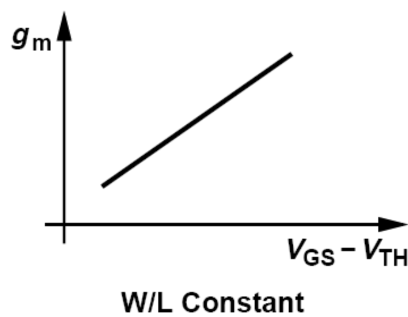


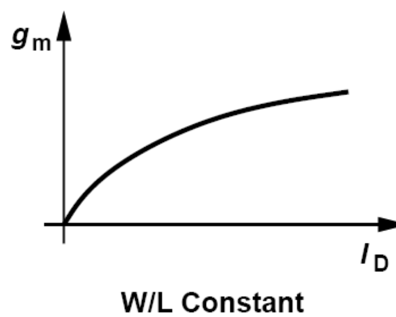
- **In saturation region, I_D is independent of V_{DS} => device acts as a current source:**

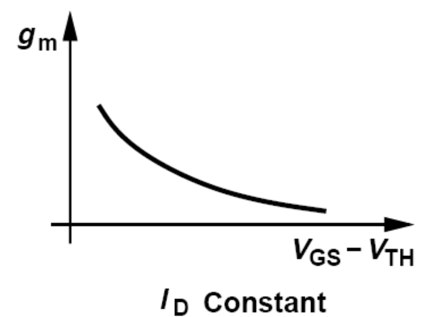


Concept of Transconductance

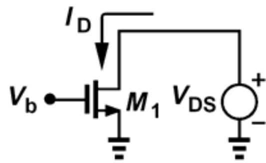
$$g_m = \frac{\partial I_D}{\partial V_{GS}}$$



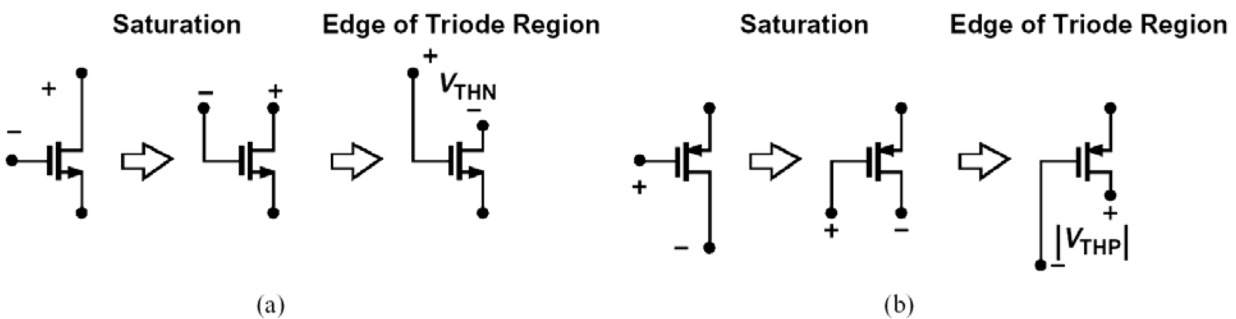




Example

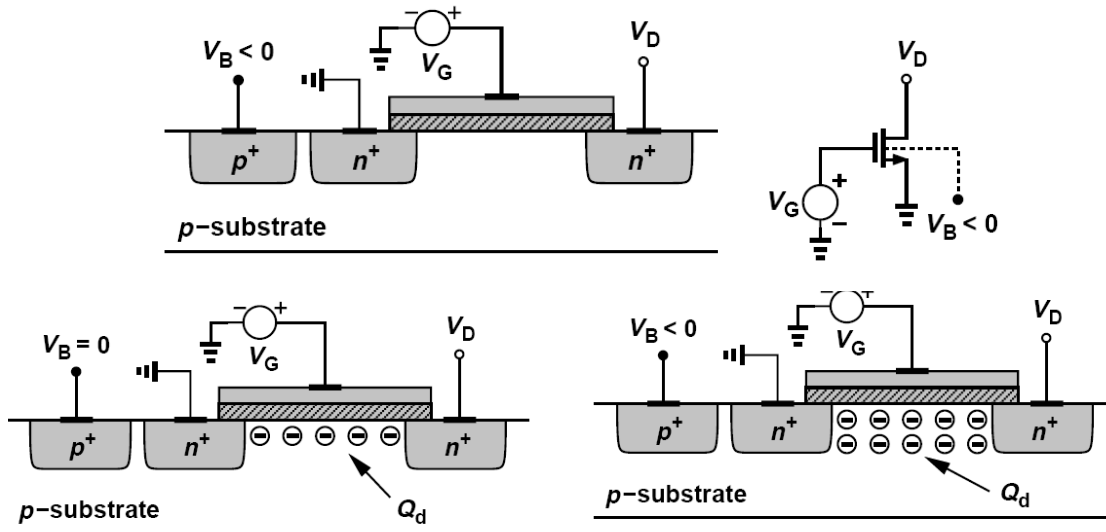


Conceptual Visualization



Other Phenomena

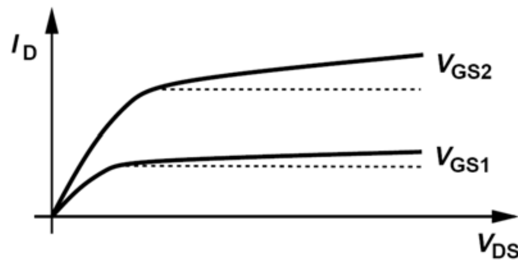
1. Body Effect:



- **As V_B becomes more negative, more holes can break loose from atoms under the gate area, leaving negative ions behind => depletion region can contribute more charge => inversion layer forms for larger V_G => threshold voltage ↑**

$$V_{TH} = V_{TH0} + \gamma(\sqrt{2\Phi_F + V_{SB}} - \sqrt{2\Phi_F}) \qquad \gamma = \sqrt{2q\epsilon_{si}N_{sub}}/C_{ox}$$

2. Channel Length Modulation



- **As V_{DS} ↑, the width of depletion region between inversion layer and drain ↑ => Effective channel length ↓ = I_D ↑**

$$I_D \approx \frac{1}{2}\mu_n C_{ox}\frac{W}{L}(V_{GS}-V_{TH})^2(1+\lambda V_{DS})$$

3. Mobility Degradation with Vertical Field

As V_{GS} ↑, vertical field ↑ => carries travel closer to interface and experience more scattering => mobility falls:

4. Mobility Degradation with Lateral Field

At high electrical fields, electrons experience substantial scattering from lattice and eventually travel at a constant velocity: $I = Q_d v$

Consequences of Velocity Saturation:

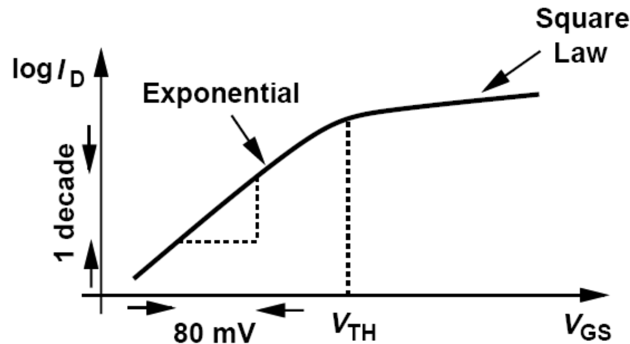
I. Drain current saturates before pinch-off => it's lower than predicted by square law.
II. Transconductance is relatively independent of current and channel length. Why?

5. Subthreshold Conduction

For V_{GS} near V_{TH}, I_D has an exponential dependence on V_{GS}:

$$I_D = I_0 \exp \frac{V_{GS}}{\zeta V_T}$$

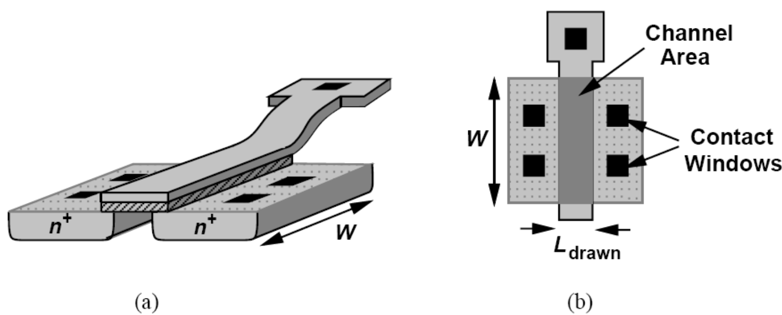
if V_{DS} is greater than roughly 200 mV. This conduction is important in very large circuits, e.g., memories, because it results in finite stand-by current.



6. Temperature Effects

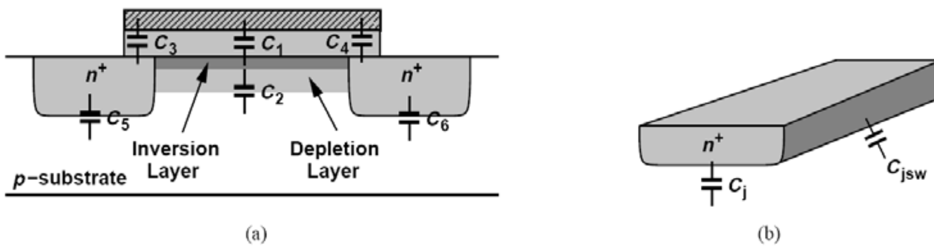
The mobility and threshold voltage vary with temperature:

Device Layout



(a) (b)

MOS Capacitances



(a) (b)

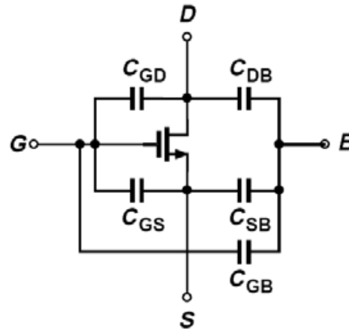
Gate – Channel Cap. **C1 =**
Gate - S/D Overlap Cap. **C2 = C3 =**

Gate – Bulk Cap. C4 =

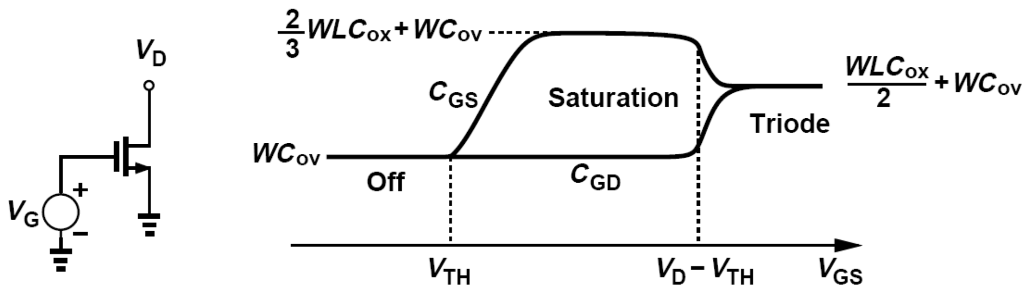
Source and drain junction caps consist of two components: sidewall and bottom plate. Each component can be expressed as:

$$C_j = C_{j0}/[1 + V_R/(2\Phi_F)]^m$$

where m is typically between 0.3 and 0.5. The device thus looks like this:

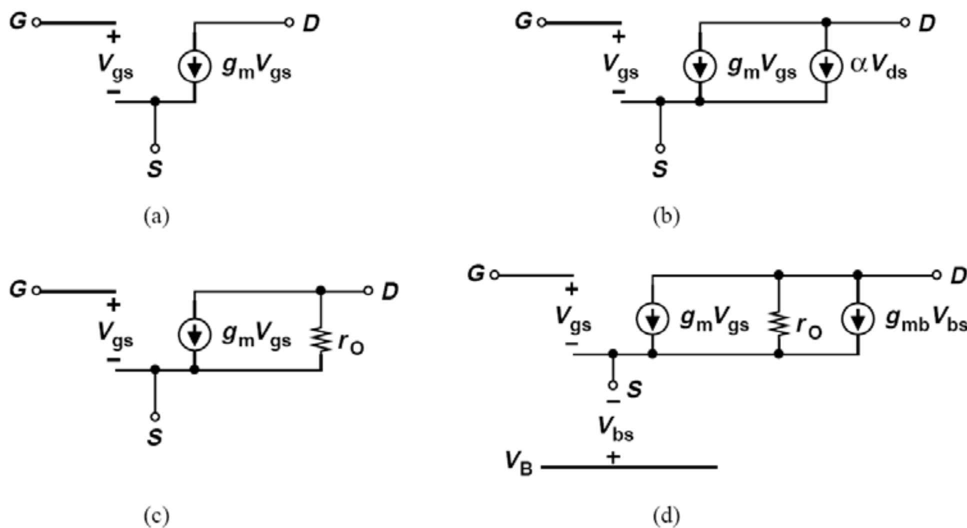


NOTE: Depending on the region of operation (off, triode, sat.), the equivalent capacitances between terminals assume different values.



Small-Signal Model

The model can be developed by perturbing the voltage difference between each two terminals and measuring each resulting current change.



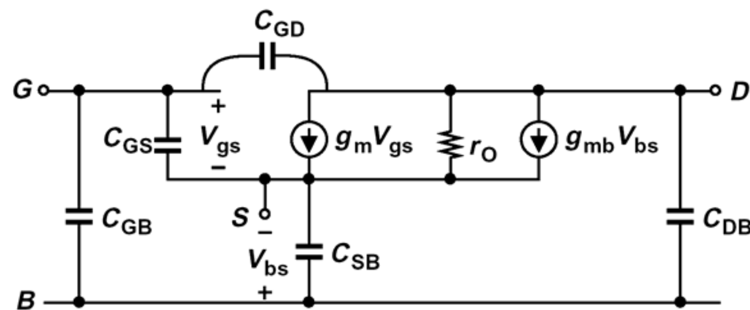
For body effect:

$$g_{mb} = \frac{\partial I_D}{\partial V_{BS}}$$
$$= \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})(-\frac{\partial V_{TH}}{\partial V_{BS}})$$

and hence:

$$g_{mb} = g_m \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}}$$
$$= \eta g_m,$$

Complete Model:



SPICE MOS Model

The following parameters are the bare minimum SPICE needs to simulate circuits.

VTO: threshold voltage with zero V_{SB}
GAMMA: body effect coefficient
PHI: $2\Phi_F$
TOX: gate oxide thickness
NSUB: substrate doping
LD: source/drain side diffusion
UO: channel mobility
LAMBDA: channel-length modulation coefficient
CJ: source/drain bottom-plate junction capacitance per unit area
CJSW: source/drain sidewall junction capacitance per unit length
PB: source/drain junction built-in potential
MJ: exponent in CJ equation
MJSW: exponent in CJSW equation
CGDO: gate-drain overlap capacitance per unit width
CGSO: gate-source overlap capacitance per unit width
JS: source/drain leakage current per unit area

Modern MOS models have several hundred parameters.