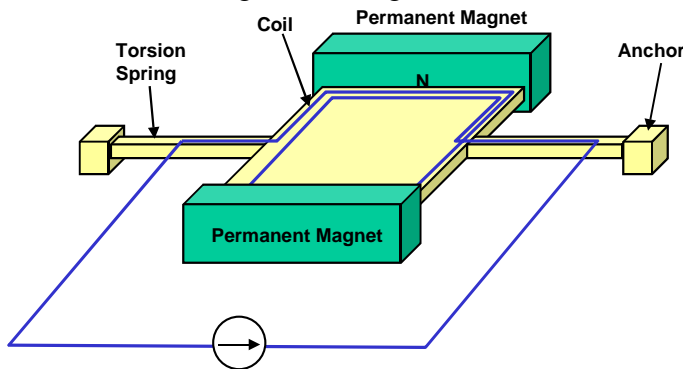


## HW#2

1) Consider the following electromagnetic actuator:



The torsion mirror shown above is driven by electromagnetic force produced by the coil in magnetic field. The magnetic field is generated by a pair of permanent magnets with magnetic flux density of  $B = 1$  Tesla. The torsion mirror made of silicon has an area of  $W \times W = 100 \times 100 \mu\text{m}^2$  and a thickness of  $10 \mu\text{m}$ , and the coil has 10 turns. For additional material parameters, use the table for Si or poly-Si in our lecture viewgraph, or Table 8.1 in Senturia's book).

- Derive the DC transfer function of the torsion mirror (rotation angle versus current).
- Construct the equivalent lumped circuit element model for the actuator, including electrical, magnetic, and the mechanical domains. The mass of the torsion plate is  $m$ .
- Solve the equivalent circuit in (a) using Kirchoff's Laws. Find the transfer function of the equivalent circuit (i.e., rotation angle as a function of input current). Compare that with the expression found in (a).
- The torsion beam is also made of Si, and is  $2 \mu\text{m}$  wide,  $10 \mu\text{m}$  thick, and  $500 \mu\text{m}$  long. Find out the compliance of the torsion spring. (Make sure you include both springs).
- Use the torsion beams in (d) and the following bias parameters, find the torque and the angular displacement of the torsion mirror:  
 $I = 10 \text{ mA}$ , Magnetic flux density  $B = 1 \text{ Tesla}$